

Exercise 5.4

Differentiate the following functions with respect to x (তলৰ ফলনসমূহ x ৰ সাপেক্ষে
অৱকলজ কৰা) :

1. $\frac{e^x}{\sin x}$

Solution : ধৰা আছ'ল, $y = \frac{e^x}{\sin x}$

$$\begin{aligned} \therefore \frac{dy}{dx} &= \frac{d}{dx} \left(\frac{e^x}{\sin x} \right) \\ &= \frac{\sin x \cdot \frac{d}{dx}(e^x) - e^x \cdot \frac{d}{dx}(\sin x)}{(\sin x)^2} \quad \left[\because \left(\frac{u}{v} \right)' = \frac{u'v - uv'}{v^2} \right] \\ &= \frac{\sin x \cdot e^x - e^x \cdot \cos x}{\sin^2 x} \\ &= \frac{e^x(\sin x - \cos x)}{\sin^2 x} \quad \underline{\text{Answer}} \end{aligned}$$

2. $e^{\sin^{-1} x}$

Solution : ধৰা আছ'ল, $y = e^{\sin^{-1} x}$

$$\begin{aligned} \therefore \frac{dy}{dx} &= \frac{d}{dx} (e^{\sin^{-1} x}) \\ &= e^{\sin^{-1} x} \cdot \frac{d}{dx} (\sin^{-1} x) \\ &= e^{\sin^{-1} x} \cdot \frac{1}{\sqrt{1-x^2}} \quad \left[\because \frac{d}{dx} (\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}} \right] \\ &= \frac{e^{\sin^{-1} x}}{\sqrt{1-x^2}} \quad \underline{\text{Answer}} \end{aligned}$$

3. e^{x^3}

Solution : ধৰা আছ'ল, $y = e^{x^3}$

$$\begin{aligned}
 \therefore \frac{dy}{dx} &= \frac{d}{dx}(e^{x^3}) \\
 &= e^{x^3} \cdot \frac{d}{dx}(x^3) && \left[\because \frac{d}{dx}(e^{mx}) = e^{mx} \cdot \frac{d}{dx}(mx) = me^{mx} \right] \\
 &= e^{x^3} \cdot 3x^2 \\
 &= 3x^2 e^{x^3} \quad \underline{\text{Answer}}
 \end{aligned}$$

4. $\sin(\tan^{-1} e^{-x})$

Solution : ধৰাহ'ল, $y = \sin(\tan^{-1} e^{-x})$

$$\begin{aligned}
 \therefore \frac{dy}{dx} &= \frac{d}{dx}\{\sin(\tan^{-1} e^{-x})\} \\
 &= \{\cos(\tan^{-1} e^{-x})\} \cdot \frac{d}{dx}(\tan^{-1} e^{-x}) && \left[\because \frac{d}{dx}(\sin mx) = \cos mx \cdot \frac{d}{dx}(mx) = m \cos mx \right] \\
 &= \{\cos(\tan^{-1} e^{-x})\} \cdot \frac{1}{1+(e^{-x})^2} \cdot \frac{d}{dx}(e^{-x}) \\
 &= \{\cos(\tan^{-1} e^{-x})\} \cdot \frac{1}{1+e^{-2x}} \cdot (-e^{-x}) && \left[\because \frac{d}{dx}(e^{-x}) = -e^{-x} \right] \\
 &= \frac{-\{\cos(\tan^{-1} e^{-x})\} e^{-x}}{1+e^{-2x}} \quad \underline{\text{Answer}}
 \end{aligned}$$

5. $\log(\cosec x)$

Solution : ধৰাহ'ল, $y = \log(\cosec x)$

$$\begin{aligned}
 \therefore \frac{dy}{dx} &= \frac{d}{dx}\{\log(\cosec x)\} \\
 &= \frac{1}{\cosec x} \cdot \frac{d}{dx}(\cosec x) && \left[\because \frac{d}{dx}(\log mx) = \frac{1}{mx} \frac{d}{dx}(mx) \right] \\
 &= \frac{1}{\cosec x} \cdot (-\sin e^x) \cdot \frac{d}{dx}(e^x) \\
 &= -\tan e^x \cdot e^x \\
 &= -e^x \tan e^x \quad \underline{\text{Answer}}
 \end{aligned}$$

A Few Home Works :

Find $\frac{dy}{dx}$ of the following functions :

1. $y = \sin(ax^2 + bx + c)$

2. $y = \tan(\sin 2x)$

3. $y = \sqrt{x^n}$

4. $y = \cos\sqrt{kx}$

5. $y = \frac{ax^3}{\sqrt{x}}$

6. $y = \frac{ax^4}{b\sqrt[5]{x}}$

7. $y = \sqrt[n]{x^7}$

8. $y = 2\sqrt{\tan(ax)}$

9. $y = \sin\{\cos(x^3)\}$

10. $y = \frac{\sin(ax+b)}{\cos(mx+n)}$

(i) Write your Name and Roll No. in the front page of your Answerscript.

[ৰেল নং আৰু নাম লিখিবা]

(ii) Send your Answerscript (containing the solutions of the above questions)

to my Email : mridulkrgogoi@gmail.com

[তোমালোকৰ উওৰ বহী সমূহ মোৰ Email ত পঠাই দিবা]